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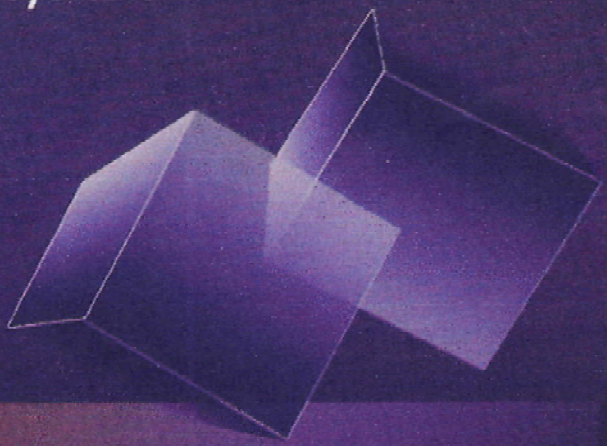
Vladimir KASIANOV

SUBJECTIVE ENTROPY OF PREFERENCES

Subjective analysis

Objects and rating preferences
Entropy maximum principle
Dynamics and conflict of preferences
Safety of active systems
Safety of flight



Warsaw 2013

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CONTENTS

APPRECIATION 7

INTRODUCTION 9

1. ACTIVE SYSTEMS 23

1.1. Active systems – introductory remarks 23
1.2. Notions and criteria of problem-resource analysis 24
1.2.1. Problem 28
1.2.2. Resources 29
1.2.3. Purposes 37
1.3. Elements of theory of individual utility 38
1.3.1. Binary relations, ordering 38
1.3.2. Determinate utility 42
1.3.3. Expected utility 46
1.4. Further analysis of the fundamental notions 48
1.4.1. Problem-resource situation 48
1.4.2. Situational dynamics 50
1.4.3. Dynamics of sets and derivative with respect to measure 51
1.4.4. Dynamics of sets and moments problem 52
1.4.5. Different sets of states 54
1.4.6. Properties of simple alternatives 59

2. INDIVIDUAL OBJECT PREFERENCES 63

2.1 Individual functions of preference, state, composition, strategy 63
2.2. Preference functions at the set of simple alternatives and their normalization 67
2.3. Normalization of complex alternatives preferences 69
2.4. Hypothesis of factorization 73
2.5. Analogy to distributions of probabilities. About the algebra of alternatives 77
2.6. Axiomatic approach to preference functions 82
2.7. About preference functions for a discrete set of alternatives S_a 84
2.8. Elements of theory of categories and its application to an analysis of active systems 86
2.8.1. Introductory remarks 86
2.8.2. The definition of category 87
2.8.3. Correspondences and mapping 88

2.8.4. Cardinal structure of sets, cardinal numbers, invariants 90
2.8.5. Invariants and variation principle in the theory of categories 92
2.9. Jensen inequality for ordered sequences 98
2.10. Subjective probability and expected utility 108
2.10.1. Relative probability 108
2.10.2. Objective utilities and subjective preferences 111

3. SUBJECTIVE ENTROPY OF INDIVIDUAL PREFERENCES. VARIATION PRINCIPLE. SUBJECTIVE INFORMATION 116

3.1. Subjective entropy 116
3.2. About non-one normalizations 119
3.3. Analogies to Shannon entropy 123
3.4. Subjective information. Entropy of ways 128
3.5. Variation principle. Canonical distributions of preferences for a discrete set of alternatives 136
3.6. Mixed type variational problems 160
3.7. On the threshold values of entropy, the moments of distributions of preferences "of switching" and "the moments of selection" 167
3.8. Entropy of ordinal distributions of preferences 172
3.9. Two optimization tasks: optimization of utilities and optimization of preferences 178

4. GROUP OF SUBJECTS. FUNCTIONS OF RATING PREFERENCES. AGGREGATION OF PREFERENCES 185

4.1. Problems, related to subjective analysis of a group of interacting subjects 185
4.2. About ordinal theory of corporative decisions. Theory of aggregate utility 187
4.3. Group of interacting subjects. Preferences functions of the 2nd kind 198
4.4. Individual ratings. Functions of group effectiveness 203
4.5. Ratings and ranks. "Well"-organized groups 219
4.6. Mutual utilities 247
4.7. Consolidation of resources in group 259
4.8. Aggregation of rating preferences 266
4.8.1. Aggregation of individual ratings 266
4.8.2. Ratings of subgroups of subjects 273
4.9. Notion of "problem" referred to a set of ranks 277
4.10. Stable imperatives. Brief survey of ethics 281
4.11. Stable imperatives in schemes of subjective analysis 290
4.12. One more time about "virtual subject" 308

4.13. Laws of supply and demand as the result of the action of the entropy principle of optimality 323
4.14. Cost of subjective information 331
4.15. Aggregation of preferences in crew of the two pilots. 341

5. DYNAMICS AND INTER INFLUENCE OF PREFERENCES 344

5.1. Problems of the analysis of dynamics and mutual influence of the preferences 344
5.2. Basic problems types of the preferences dynamics 348
5.3. Exogenous dynamics of the I type preferences 349
5.4. Reciprocal effect of the individual preferences in the group 358
5.5. A priori and a posteriori preferences of the I type. "The chains of distributions" 367
5.5.1. Accounting of the influence of a priori preferences 367
5.5.2. The canonical distributions of the I type preferences expressed through the „speeds" of the resources conversions 376
5.6. Models of endogenous dynamics of the active systems 378
5.7. Simulation of the preferences dynamics of the first kind and exogenous processes 406
5.7.1. Dynamics of the consumer's preferences by the exogenous model of Walras - Leontyev 406
5.7.2. Dynamics of the preferences of consumer and producer with the Walras - Leontyev's exogenous model 414
5.7.3. Model of the appearance of the stress states of the consumer 420
5.8. Elasticity and rigidity of preferences – elasticity and the rigidity of psychics. Sensitivity of preferences 428
5.9. Alternation of the problem- resource situation in the course of decision making on the self of alternatives 442
5.10. Ratings dynamics. Joint dynamics of the preferences of I and II type 450
5.11. On a change in the number of alternatives 464
5.12. "Manipulation on consciousness" – dynamical process of preferences modifications 469
5.13. Some additional tasks 475
5.13.1. Beast – victim – hunter 475
5.13.2. On the models of advertising campaign 480
5.13.3. Auto-relaxation of the preferences distributions 485
5.13.4. Complete Walras - Leontev model, including preferences of consumer and producer 492
5.13.5. Competition of ideas. One model of the sociodynamics 496

6. SAFETY OF THE ACTIVE SYSTEMS 505

6.1. Approach to a study of the active systems safety 505
6.2. "Dangers" and "threats" 513
6.3. Flight safety and the subjective analysis 517
6.4. Probabilistic flight models. Combining of the probabilistic and subjective analysis 534

7. CONFLICTS, COGNITIVE DISSONANCE, SUBJECTIVE FREEDOM 554

7.1. Conflicts from the point of view of the subjective analysis 554
7.2. Model characteristics of the internal conflict 564
7.2.1. Utilitarian internal conflicts 564
7.2.2. Internal ethical conflicts 574
7.3. Model characteristics of the intersubject conflict 578
7.4. Entropy map 589
7.4.1. On the quantization of the preferences 589
7.4.2. What is an entropy map? 591
7.5. Category „freedom" from the point of view of subjective analysis. Brief historical excursus 598
7.6. Evolution of the conflicts 611
7.7. Dynamics of the „living points" 618

BIBLIOGRAPHY 634